



# PKCS #1 v2.1: RSA Cryptography Standard

RSA Laboratories

DRAFT 1 — September 17, 1999

Editor’s note: This is the first draft of PKCS #9 v2.1, which is available for a 30-day public review period. Please send comments and suggestions, both technical and editorial, to [pkcs-editor@rsasecurity.com](mailto:pkcs-editor@rsasecurity.com) or [pkcs-tng@rsasecurity.com](mailto:pkcs-tng@rsasecurity.com).

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## 1. Introduction

This document provides recommendations for the implementation of public-key cryptography based on the RSA algorithm [25], covering the following aspects:

- cryptographic primitives
- encryption schemes
- signature schemes with appendix
- ASN.1 syntax for representing keys and for identifying the schemes

The recommendations are intended for general application within computer and communications systems, and as such include a fair amount of flexibility. It is expected that application standards based on these specifications may include additional constraints. The recommendations are intended to be compatible with draft standards currently being developed by the ANSI X9F1 [1] and IEEE P1363 working groups [19].

This document supersedes PKCS #1 version 2.0 [27] but includes compatible techniques.

*Editor's note.* It is expected that subsequent versions of PKCS #1 may cover other aspects of the RSA algorithm such as key size, key generation, key validation, and signature schemes with message recovery.

## 1.1 Overview

The organization of this document is as follows:

- Section 1 is an introduction.
- Section 2 defines some notation used in this document.
- Section 3 defines the RSA public and private key types.
- Sections 4 and 5 define several primitives, or basic mathematical operations. Data conversion primitives are in Section 4, and cryptographic primitives (encryption-decryption, signature-verification) are in Section 5.
- Sections 6, 7 and 8 deal with the encryption and signature schemes in this document. Section 6 gives an overview. Along with the methods found in PKCS #1 v1.5, Section 7 defines an OAEP-based [2] encryption scheme and Section 8 defines a PSS-based [3][4] signature scheme with appendix.
- Section ~~09~~ defines the encoding methods for the encryption and signature schemes in Sections 7 and 8.
- Appendix A defines the ASN.1 syntax for the keys defined in Section 3 and the schemes in Sections 7 and 8.
- Appendix B defines the hash functions and the mask generation function used in this document, including ASN.1 syntax for the techniques.
- Appendix C gives an ASN.1 module.
- Appendices D, E, F and G cover intellectual property issues, outline the revision history of PKCS #1, give references to other publications and standards, and provide general information about the Public-Key Cryptography Standards.

## 2. Notation

$(n, e)$	RSA public key
$c$	ciphertext representative, an integer between 0 and $n-1$
$C$	ciphertext, an octet string
$d$	private exponent
$dP$	$p$ 's exponent, a positive integer such that: $e \cdot dP \equiv 1 \pmod{(p-1)}$
$dQ$	$q$ 's exponent, a positive integer such that: $e \cdot dQ \equiv 1 \pmod{(q-1)}$
$e$	public exponent
$EM$	encoded message, an octet string
$emLen$	(intended) length in octets of an encoded message $EM$
$\text{GCD}(\cdot, \cdot)$	greatest common divisor of two nonnegative integers
$H$	hash value, an output of $Hash$
$Hash$	hash function
$hLen$	output length in octets of hash function $Hash$
$k$	length in octets of the modulus
$K$	RSA private key
$l$	intended length of octet string
$\text{LCM}(\cdot, \cdot)$	least common multiple of two nonnegative integers
$m$	message representative, an integer between 0 and $n-1$
$M$	message, an octet string
$mask$	mask, an octet string
$mLen$	length in octets of a message $M$

<i>MGF</i>	mask generation function
<i>mLen</i>	length in octets of a message
<i>n</i>	modulus
<i>P</i>	encoding parameters, an octet string
<i>p, q</i>	prime factors of the modulus
<i>qInv</i>	CRT coefficient, a positive integer less than <i>p</i> such that: $q \cdot qInv \equiv 1 \pmod{p}$
<i>s</i>	signature representative, an integer between 0 and <i>n</i> -1
<i>S</i>	signature, an octet string
<i>salt</i>	salt value, an octet string
<i>x</i>	a nonnegative integer
<i>X</i>	an octet string corresponding to <i>x</i>
xor	bitwise exclusive-or of two octet strings
<i>Z</i>	seed from which mask is generated, an octet string
$\lambda(n)$	LCM ( <i>p</i> -1, <i>q</i> -1), where $n = p \cdot q$
	concatenation operator
·	octet length operator

### 3. Key types

Two key types are employed in the primitives and schemes defined in this document: *RSA public key* and *RSA private key*. Together, an RSA public key and an RSA private key form an *RSA key pair*.

#### 3.1 RSA public key

For the purposes of this document, an RSA public key consists of two components:

- *n*, the modulus, a nonnegative integer
- *e*, the public exponent, a nonnegative integer

In a *valid RSA public key*, the modulus  $n$  is a product of two odd primes  $p$  and  $q$ , and the public exponent  $e$  is an integer between 3 and  $n-1$  satisfying  $\text{GCD}(e, \lambda(n)) = 1$ , where  $\lambda(n) = \text{LCM}(p-1, q-1)$ .

A recommended syntax for interchanging RSA public keys between implementations is given in Appendix A.1.1; an implementation's internal representation may differ.

### 3.2 RSA private key

For the purposes of this document, an RSA private key may have either of two representations.

1. The first representation consists of the pair  $(n, d)$ , where the components have the following meanings:

- $n$ , the modulus, a nonnegative integer
- $d$ , the private exponent, a nonnegative integer

2. The second representation consists of a quintuple  $(p, q, dP, dQ, qInv)$ , where the components have the following meanings:

- $p$ , the first factor, a nonnegative integer
- $q$ , the second factor, a nonnegative integer
- $dP$ , the first factor's exponent, a nonnegative integer
- $dQ$ , the second factor's exponent, a nonnegative integer
- $qInv$ , the CRT coefficient, a nonnegative integer

In a *valid RSA private key* with the first representation, the modulus  $n$  is the same as in the corresponding public key and is the product of two odd primes  $p$  and  $q$ , and the private exponent  $d$  is a positive integer less than  $n$  satisfying

$$e \cdot d \equiv 1 \pmod{\lambda(n)}$$

where  $e$  is the corresponding public exponent and  $\lambda(n)$  is as defined above.

In a *valid RSA private key* with the second representation, the two factors  $p$  and  $q$  are the prime factors of the modulus  $n$ , the exponents  $dP$  and  $dQ$  are positive integers less than  $p$  and  $q$  respectively satisfying

$$\begin{aligned} e \cdot dP &\equiv 1 \pmod{p-1} \\ e \cdot dQ &\equiv 1 \pmod{q-1}, \end{aligned}$$

and the CRT coefficient  $qInv$  is a positive integer less than  $p$  satisfying

$$q \cdot qInv \equiv 1 \pmod{p}.$$

A recommended syntax for interchanging RSA private keys between implementations, which includes components from both representations, is given in Appendix A.1.2; an implementation's internal representation may differ.

## 4. Data conversion primitives

Two data conversion primitives are employed in the schemes defined in this document:

- I2OSP – Integer-to-Octet-String primitive
- OS2IP – Octet-String-to-Integer primitive

For the purposes of this document, and consistent with ASN.1 syntax, an octet string is an ordered sequence of octets (eight-bit bytes). The sequence is indexed from first (conventionally, leftmost) to last (rightmost). For purposes of conversion to and from integers, the first octet is considered the most significant in the following conversion primitives

### 4.1 I2OSP

I2OSP converts a nonnegative integer to an octet string of a specified length.

I2OSP ( $x, l$ )

*Input:*         $x$         nonnegative integer to be converted

$l$         intended length of the resulting octet string

*Output:*        $X$         corresponding octet string of length  $l$

*Errors:*        “integer too large”

*Steps:*

1.     If  $x \geq 256^l$ , output “integer too large” and stop.
2.     Write the integer  $x$  in its unique  $l$ -digit representation base 256:

$$x = x_{l-1} 256^{l-1} + x_{l-2} 256^{l-2} + \dots + x_1 256 + x_0$$

where  $0 \leq x_i < 256$  (note that one or more leading digits will be zero if  $x < 256^{l-1}$ ).

3. Let the octet  $X_i$  have the value  $x_{l-i}$  for  $1 \leq i \leq l$ . Output the octet string

$$X = X_1 X_2 \dots X_l.$$

## 4.2 OS2IP

OS2IP converts an octet string to a nonnegative integer.

OS2IP ( $X$ )

*Input:*  $X$  octet string to be converted

*Output:*  $x$  corresponding nonnegative integer

*Steps:*

1. Let  $X_1 X_2 \dots X_l$  be the octets of  $X$  from first to last, and let  $x_{l-i}$  have value  $X_i$  for  $1 \leq i \leq l$ .
2. Let  $x = x_{l-1} 256^{l-1} + x_{l-2} 256^{l-2} + \dots + x_1 256 + x_0$ .
3. Output  $x$ .

## 5. Cryptographic primitives

Cryptographic primitives are basic mathematical operations on which cryptographic schemes can be built. They are intended for implementation in hardware or as software modules, and are not intended to provide security apart from a scheme.

Four types of primitive are specified in this document, organized in pairs: encryption and decryption; and signature and verification.

The specifications of the primitives assume that certain conditions are met by the inputs, in particular that public and private keys are valid.

### 5.1 Encryption and decryption primitives

An encryption primitive produces a ciphertext representative from a message representative under the control of a public key, and a decryption primitive recovers the message representative from the ciphertext representative under the control of the corresponding private key.

One pair of encryption and decryption primitives is employed in the encryption schemes defined in this document and is specified here: RSAEP/RSADP. RSAEP and RSADP involve the same mathematical operation, with different keys as input.



The primitives defined here are the same as in the IEEE P1363 draft [19] and are compatible with PKCS #1 v1.5.

The main mathematical operation in each primitive is exponentiation.

### 5.1.1 RSAEP

RSAEP  $((n, e), m)$

*Input:*  $(n, e)$  RSA public key

$m$  message representative, an integer between 0 and  $n-1$

*Output:*  $c$  ciphertext representative, an integer between 0 and  $n-1$

*Errors:* “message representative out of range”

*Assumptions:* public key  $(n, e)$  is valid

*Steps:*

1. If the message representative  $m$  is not between 0 and  $n-1$ , output “message representative out of range” and stop.
2. Let  $c = m^e \bmod n$ .
3. Output  $c$ .

### 5.1.2 RSADP

RSADP  $(K, c)$

*Input:*  $K$  RSA private key, where  $K$  has one of the following forms:

— a pair  $(n, d)$

— a quintuple  $(p, q, dP, dQ, qInv)$

$c$  ciphertext representative, an integer between 0 and  $n-1$

*Output:*  $m$  message representative, an integer between 0 and  $n-1$

*Errors:* “ciphertext representative out of range”

*Assumptions:* private key  $K$  is valid

*Steps:*

1. If the ciphertext representative  $c$  is not between 0 and  $n-1$ , output “ciphertext representative out of range” and stop.
2. If the first form  $(n, d)$  of  $K$  is used:
  - 2.1 Let  $m = c^d \bmod n$ .
 Else, if the second form  $(p, q, dP, dQ, qInv)$  of  $K$  is used:
  - 2.2 Let  $m_1 = c^{dP} \bmod p$ .
  - 2.3 Let  $m_2 = c^{dQ} \bmod q$ .
  - 2.4 Let  $h = qInv (m_1 - m_2) \bmod p$ .
  - 2.5 Let  $m = m_2 + h q$ .
3. Output  $m$ .

## 5.2 Signature and verification primitives

A signature primitive produces a signature representative from a message representative under the control of a private key, and a verification primitive recovers the message representative from the signature representative under the control of the corresponding public key. One pair of signature and verification primitives is employed in the signature schemes defined in this document and is specified here: RSASP1/RSVP1.

The primitives defined here are the same as in the IEEE P1363 draft and are compatible with PKCS #1 v1.5.

The main mathematical operation in each primitive is exponentiation, as in the encryption and decryption primitives of Section 5.1. RSASP1 and RSVP1 are the same as RSADP and RSAEP except for the names of their input and output arguments; they are distinguished as they are intended for different purposes.

### 5.2.1 RSASP1

RSASP1 ( $K, m$ )

*Input:*  $K$  RSA private key, where  $K$  has one of the following forms:

- a pair  $(n, d)$
- a quintuple  $(p, q, dP, dQ, qInv)$

$m$  message representative, an integer between 0 and  $n-1$

*Output:*  $s$  signature representative, an integer between 0 and  $n-1$

*Errors:* “message representative out of range”

*Assumptions:* private key  $K$  is valid

*Steps:*

1. If the message representative  $m$  is not between 0 and  $n-1$ , output “message representative out of range” and stop.
2. If the first form  $(n, d)$  of  $K$  is used:
  - 2.1 Let  $s = m^d \bmod n$ .
 Else, if the second form  $(p, q, dP, dQ, qInv)$  of  $K$  is used:
  - 2.2 Let  $s_1 = m^{dP} \bmod p$ .
  - 2.3 Let  $s_2 = m^{dQ} \bmod q$ .
  - 2.4 Let  $h = qInv (s_1 - s_2) \bmod p$ .
  - 2.5 Let  $s = s_2 + h q$ .
3. Output  $s$ .

### 5.2.2 RSAVP1

RSAVP1  $((n, e), s)$

*Input:*  $(n, e)$  RSA public key

$s$  signature representative, an integer between 0 and  $n-1$

*Output:*  $m$  message representative, an integer between 0 and  $n-1$

*Errors:* “signature representative out of range”

*Assumptions:* public key  $(n, e)$  is valid

*Steps:*

1. If the signature representative  $s$  is not between 0 and  $n-1$ , output “signature representative out of range” and stop.
2. Let  $m = s^e \bmod n$ .

3. Output  $m$ .

## 6. Overview of schemes

A scheme combines cryptographic primitives and other techniques to achieve a particular security goal. Two types of scheme are specified in this document: encryption schemes and signature schemes with appendix.

The schemes specified in this document are limited in scope in that their operations consist only of steps to process data with a key, and do not include steps for obtaining or validating the key. Thus, in addition to the scheme operations, an application will typically include key management operations by which parties may select public and private keys for a scheme operation. The specific additional operations and other details are outside the scope of this document.

As was the case for the cryptographic primitives (Section 5), the specifications of scheme operations assume that certain conditions are met by the inputs, in particular that public and private keys are valid. The behavior of an implementation is thus unspecified when a key is invalid. The impact of such unspecified behavior depends on the application. Possible means of addressing key validation include explicit key validation by the application; key validation within the public-key infrastructure; and assignment of liability for operations performed with an invalid key to the party who generated the key.

A generally good cryptographic practice is to employ a given key pair in only one scheme. This avoids the risk that a vulnerability in one scheme may compromise the security of the other, and may be essential to maintain provable security. As an example, suppose a key pair is employed in both RSAES-OAEP (Section 7.1) and RSAES-PKCS1-v1\_5 (Section 7.2). Although RSAES-OAEP by itself would resist attack, an opponent could exploit a vulnerability in the implementation of RSAES-PKCS1-v1\_5 to recover messages encrypted with either scheme. As another example, suppose a key pair is employed in both RSASSA-PKCS1-v1\_5 (Section 8.1) and RSASSA-PSS (Section 8.2). Then the security proof for RSASSA-PSS would no longer be sufficient since the proof does not account for the possibility the signatures might be generated with a second scheme. No vulnerability is apparent in this case but the proof of security is lost. Similar considerations may apply if a key pair is employed in one of the schemes defined here and a variant defined elsewhere.

There may be situations in which only one key pair is available and it needs to be employed in multiple schemes, e.g., an encryption and a signature scheme. In such a case, additional security evaluation is necessary. RSAES-OAEP and RSASSA-PSS are designed in a way that prevents an opponent from exploiting interactions between the schemes, so would be appropriate for such a situation. RSAES-PKCS1-v1\_5 and RSASSA-PKCS1-v1\_5 have traditionally been employed together (indeed, this is the model introduced by PKCS #1 v1.5), without any known bad interactions. But in general, it is prudent to limit a key pair to a single scheme and purpose.

## 7. Encryption schemes

An *encryption scheme* consists of an *encryption operation* and a *decryption operation*, where the encryption operation produces a ciphertext from a message with a recipient's public key, and the decryption operation recovers the message from the ciphertext with the recipient's corresponding private key.

An encryption scheme can be employed in a variety of applications. A typical application is a key establishment protocol, where the message contains key material to be delivered confidentially from one party to another. For instance, PKCS #7 [28] employs such a protocol to deliver a content-encryption key from a sender to a recipient; the encryption schemes defined here would be suitable key-encryption algorithms in that context.

Two encryption schemes are specified in this document: RSAES-OAEP and RSAES-PKCS1-v1\_5. RSAES-OAEP is recommended for new applications; RSAES-PKCS1-v1\_5 is included only for compatibility with existing applications, and is not recommended for new applications.

The encryption schemes given here follow a general model similar to that employed in the IEEE P1363 draft, by combining encryption and decryption primitives with an *encoding method* for encryption. The encryption operations apply a message encoding operation to a message to produce an encoded message, which is then converted to an integer message representative. An encryption primitive is applied to the message representative to produce the ciphertext. Reversing this, the decryption operations apply a decryption primitive to the ciphertext to recover a message representative, which is then converted to an octet string encoded message. A message decoding operation is applied to the encoded message to recover the message and verify the correctness of the decryption.

### 7.1 RSAES-OAEP

RSAES-OAEP combines the RSAEP and RSADP primitives (Sections 5.1.1 and 5.1.2) with the EME-OAEP encoding method (Section 9.1.1). EME-OAEP is based on the method found in [2]. It is compatible with the IFES scheme defined in the IEEE P1363 draft where the encryption and decryption primitives are IFEP-RSA and IFDP-RSA and the message encoding method is EME-OAEP. RSAES-OAEP can operate on messages of length up to  $k-2-2hLen$  octets, where  $hLen$  is the length of the hash function output for EME-OAEP and  $k$  is the length in octets of the recipient's RSA modulus.

Assuming that the hash function in EME-OAEP has appropriate properties, and the key size is sufficiently large, RSAEP-OAEP provides "plaintext-aware encryption," meaning that it is computationally infeasible to obtain full or partial information about a message from a ciphertext, and computationally infeasible to generate a valid ciphertext without knowing the corresponding message. Therefore, a chosen ciphertext attack is ineffective against a plaintext-aware encryption scheme such as RSAES-OAEP. We briefly note that to receive the full security benefit of RSAES-OAEP, it should not be used in a protocol

involving RSAES-PKCS1-v1\_5. It is possible that in a protocol in which both encryption schemes are present, an adaptive chosen ciphertext attack such as [5] would be useful.

Both the encryption and the decryption operations of RSAES-OAEP take the value of the parameter string  $P$  as input. In this version of PKCS #1,  $P$  is an octet string that is specified explicitly. See Appendix A.2.1 for the relevant ASN.1 syntax.

### 7.1.1 Encryption operation

RSAES-OAEP-ENCRYPT  $((n, e), M, P)$

*Input:*

- $(n, e)$  recipient's RSA public key
- $M$  message to be encrypted, an octet string of length at most  $k-2-2hLen$ , where  $k$  is the length in octets of the modulus  $n$  and  $hLen$  is the length in octets of the hash function output for EME-OAEP
- $P$  encoding parameters, an octet string that may be empty

*Output:*  $C$  ciphertext, an octet string of length  $k$

*Errors:* "message too long"

*Assumptions:* public key  $(n, e)$  is valid

*Steps:*

1. Apply the EME-OAEP encoding operation (Section 9.1.1.2) to the message  $M$  and the encoding parameters  $P$  to produce an encoded message  $EM$  of length  $k-1$  octets:

$$EM = \text{EME-OAEP-ENCODE}(M, P, k-1).$$

If the encoding operation outputs "message too long," then output "message too long" and stop.

2. Convert the encoded message  $EM$  to an integer message representative  $m$ :

$$m = \text{OS2IP}(EM).$$

3. Apply the RSAEP encryption primitive (Section 5.1.1) to the public key  $(n, e)$  and the message representative  $m$  to produce an integer ciphertext representative  $c$ :

$$c = \text{RSAEP}((n, e), m).$$

4. Convert the ciphertext representative  $c$  to a ciphertext  $C$  of length  $k$  octets:

$$C = \text{I2OSP}(c, k) .$$

5. Output the ciphertext  $C$ .

### 7.1.2 Decryption operation

$\text{RSAES-OAEP-DECRYPT}(K, C, P)$

*Input:*

- $K$  recipient's RSA private key
- $C$  ciphertext to be decrypted, an octet string of length  $k$ , where  $k$  is the length in octets of the modulus  $n$
- $P$  encoding parameters, an octet string that may be empty

*Output:*  $M$  message, an octet string of length at most  $k-2-2hLen$ , where  $hLen$  is the length in octets of the hash function output for EME-OAEP

*Errors:* "decryption error"

*Steps:*

1. If the length of the ciphertext  $C$  is not  $k$  octets, output "decryption error" and stop.
2. Convert the ciphertext  $C$  to an integer ciphertext representative  $c$ :

$$c = \text{OS2IP}(C) .$$

3. Apply the RSADP decryption primitive (Section 5.1.2) to the private key  $K$  and the ciphertext representative  $c$  to produce an integer message representative  $m$ :

$$m = \text{RSADP}(K, c) .$$

If RSADP outputs "ciphertext out of range," then output "decryption error" and stop.

4. Convert the message representative  $m$  to an encoded message  $EM$  of length  $k-1$  octets:

$$EM = \text{I2OSP}(m, k-1) .$$

If I2OSP outputs "integer too large," then output "decryption error" and stop.

5. Apply the EME-OAEP decoding operation to the encoded message  $EM$  and the encoding parameters  $P$  to recover a message  $M$ :

$$M = \text{EME-OAEP-DECODE}(EM, P) .$$

If the decoding operation outputs “decoding error,” then output “decryption error” and stop.

6. Output the message  $M$ .

*Note.* It is important that the error messages output in steps 4 and 5 be the same, otherwise an adversary may be able to extract useful information from the type of error message received. Error message information is used to mount a chosen ciphertext attack on PKCS #1 v1.5 encrypted messages in [5].

## 7.2 RSAES-PKCS1-v1\_5

RSAES-PKCS1-v1\_5 combines the RSAEP and RSADP primitives with the EME-PKCS1-v1\_5 encoding method. It is the same as the encryption scheme in PKCS #1 v1.5. RSAES-PKCS1-v1\_5 can operate on messages of length up to  $k-11$  octets, although care should be taken to avoid certain attacks on low-exponent RSA due to Coppersmith, et al. when long messages are encrypted (see the third bullet in the notes below and [7]).

RSAES-PKCS1-v1\_5 does not provide “plaintext-aware” encryption. In particular, it is possible to generate valid ciphertexts without knowing the corresponding plaintexts, with a reasonable probability of success. This ability can be exploited in a chosen ciphertext attack as shown in [5]. Therefore, if RSAES-PKCS1-v1\_5 is to be used, certain easily implemented countermeasures should be taken to thwart the attack found in [5]. The addition of structure to the data to be encoded, rigorous checking of PKCS #1 v1.5 conformance and other redundancy in decrypted messages, and the consolidation of error messages in a client-server protocol based on PKCS #1 v1.5 can all be effective countermeasures and don’t involve changes to a PKCS #1 v1.5-based protocol. These and other countermeasures are discussed in [6].

*Notes.* The following passages describe some security recommendations pertaining to the use of RSAES-PKCS1-v1\_5. Recommendations from version 1.5 of this document are included as well as new recommendations motivated by cryptanalytic advances made in the intervening years.

- It is recommended that the pseudorandom octets in EME-PKCS1-v1\_5 be generated independently for each encryption process, especially if the same data is input to more than one encryption process. Hastad’s results [16] are one motivation for this recommendation.
- The padding string  $PS$  in EME-PKCS1-v1\_5 is at least eight octets long, which is a security condition for public-key operations that prevents an attacker from recovering data by trying all possible encryption blocks.
- The pseudorandom octets can also help thwart an attack due to Coppersmith et al. [7] when the size of the message to be encrypted is kept small. The attack works on low-exponent RSA when similar messages are encrypted with the same public key. More specifically, in one flavor of the attack, when two inputs to RSAEP agree on a large fraction of bits (8/9) and low-exponent RSA ( $e = 3$ ) is used to encrypt both of them, it may be possible to recover both inputs with the attack. Another flavor of the attack is successful in decrypting a single ciphertext when a large fraction (2/3) of the input to RSAEP is already known. For typical applications, the message to be encrypted is short (e.g., a 128-bit symmetric key) so not enough information will be known or common between two messages to enable the attack. However, if a long message is encrypted, or if part of a message is



known, then the attack may be a concern. In any case, the RSAEP-OAEP scheme overcomes the attack.

### 7.2.1 Encryption operation

RSAES-PKCS1-v1\_5-ENCRYPT  $((n, e), M)$

*Input:*  $(n, e)$  recipient's RSA public key  
 $M$  message to be encrypted, an octet string of length at most  $k-11$  octets, where  $k$  is the length in octets of the modulus  $n$

*Output:*  $C$  ciphertext, an octet string of length  $k$

*Errors:* "message too long"

*Steps:*

1. Apply the EME-PKCS1-v1\_5 encoding operation (Section 9.1.2.1) to the message  $M$  to produce an encoded message  $EM$  of length  $k-1$  octets:

$$EM = \text{EME-PKCS1-v1_5-ENCODE}(M, k-1) .$$

If the encoding operation outputs "message too long," then output "message too long" and stop.

2. Convert the encoded message  $EM$  to an integer message representative  $m$ :

$$m = \text{OS2IP}(EM) .$$

3. Apply the RSAEP encryption primitive (Section 5.1.1) to the public key  $(n, e)$  and the message representative  $m$  to produce an integer ciphertext representative  $c$ :

$$c = \text{RSAEP}((n, e), m) .$$

4. Convert the ciphertext representative  $c$  to a ciphertext  $C$  of length  $k$  octets:

$$C = \text{I2OSP}(c, k) .$$

5. Output the ciphertext  $C$ .

### 7.2.2 Decryption operation

RSAES-PKCS1-v1\_5-DECRYPT  $(K, C)$

*Input:*  $K$  recipient's RSA private key

$C$  ciphertext to be decrypted, an octet string of length  $k$ , where  $k$  is the length in octets of the modulus  $n$

*Output:*  $M$  message, an octet string of length at most  $k-1$

*Errors:* “decryption error”

*Steps:*

1. If the length of the ciphertext  $C$  is not  $k$  octets, output “decryption error” and stop.
2. Convert the ciphertext  $C$  to an integer ciphertext representative  $c$ :

$$c = \text{OS2IP}(C) .$$

3. Apply the RSADP decryption primitive to the private key  $(n, d)$  and the ciphertext representative  $c$  to produce an integer message representative  $m$ :

$$m = \text{RSADP}((n, d), c) .$$

If RSADP outputs “ciphertext out of range,” then output “decryption error” and stop.

4. Convert the message representative  $m$  to an encoded message  $EM$  of length  $k-1$  octets:

$$EM = \text{I2OSP}(m, k-1) .$$

If I2OSP outputs “integer too large,” then output “decryption error” and stop.

5. Apply the EME-PKCS1-v1\_5 decoding operation to the encoded message  $EM$  to recover a message  $M$ :

$$M = \text{EME-PKCS1-v1_5-DECODE}(EM) .$$

If the decoding operation outputs “decoding error,” then output “decryption error” and stop.

6. Output the message  $M$ .

*Note.* It is important that only one type of error message is output by EME-PKCS1-v1\_5, as ensured by steps 4 and 5. If this is not done, then an adversary may be able to use information extracted from the type of error message received to mount a chosen ciphertext attack such as the one found in [5].

## 8. Signature schemes with appendix

A *signature scheme with appendix* consists of a *signature generation operation* and a *signature verification operation*, where the signature generation operation produces a

signature from a message with a signer's private key, and the signature verification operation verifies the signature on the message with the signer's corresponding public key. To verify a signature constructed with this type of scheme it is necessary to have the message itself. In this way, signature schemes with appendix are distinguished from signature schemes with message recovery, which are not supported in this document.

A signature scheme with appendix can be employed in a variety of applications. For instance, the signature scheme with appendix defined here would be a suitable signature algorithm for X.509 certificates [20]. A related signature scheme could be employed in PKCS #7 [28], although for technical reasons, the current version of PKCS #7 separates a hash function from a signature scheme, which is different than what is done here.

Two signature schemes with appendix are specified in this document: RSASSA-PKCS1-v1\_5 and RSASSA-PSS. Although no attacks are known against RSASSA-PKCS1-v1\_5, in the interest of increased robustness, RSASSA-PSS is recommended for eventual adoption in new applications. RSASSA-PKCS1-v1\_5 is included for compatibility with existing applications, and while still appropriate for new applications, a gradual transition to RSASSA-PSS is encouraged.

The signature schemes with appendix given here follow a general model similar to that employed in the IEEE P1363 draft, by combining signature and verification primitives with an encoding method for signatures. The signature generation operations apply a message encoding operation to a message to produce an encoded message, which is then converted to an integer message representative. A signature primitive is then applied to the message representative to produce the signature. The signature verification operations apply a signature verification primitive to the signature to recover a message representative, which is then converted to an octet string. If the encoding method is deterministic (e.g., EMSA-PKCS1-v1\_5), the message encoding operation is again applied to the message and the result is compared to the recovered octet string. If there is a match, the signature is considered valid. If the method is randomized (e.g., EMSA-PSS), a verification operation is applied to the message and the octet string to determine whether they are consistent. (Note that this approach assumes that the signature and verification primitives have the message-recovery form. The signature generation and verification operations have a different form in the IEEE P1363 draft for other primitives.)

## 8.1 RSASSA-PKCS1-v1\_5

RSASSA-PKCS1-v1\_5 combines the RSASP1 and RSAVP1 primitives with the EMSA-PKCS1-v1\_5 encoding method. It is compatible with the IFSSA scheme defined in the IEEE P1363 draft where the signature and verification primitives are IFSP-RSA1 and IFVP-RSA1 and the message encoding method is EMSA-PKCS1-v1\_5 (which is not defined in the IEEE P1363 draft). The length of messages on which RSASSA-PKCS1-v1\_5 can operate is either unrestricted or constrained by a very large number, depending on the hash function underlying the EMSA-PKCS1-v1\_5 method.

Assuming that the hash function in EMSA-PKCS1-v1\_5 has appropriate properties and the key size is sufficiently large, RSASSA-PKCS1-v1\_5 provides secure signatures, meaning that it is computationally infeasible to generate a signature without knowing the private key, and computationally infeasible to find a message with a given signature or two messages with the same signature. Also, in the encoding method EMSA-PKCS1-v1\_5, a hash function identifier is embedded in the encoding. Because of this feature, an adversary must invert or find collisions of the particular hash function being used; attacking a different hash function than the one selected by the signer is not useful to the adversary.

*Notes.*

1. As noted in PKCS #1 v1.5, the EMSA-PKCS1-v1\_5 encoding method has the property that the encoded message, converted to an integer message representative, is guaranteed to be large and at least somewhat “random”. This prevents attacks of the kind proposed by Desmedt and Odlyzko [12] where multiplicative relationships between message representatives are developed by factoring the message representatives into a set of small values (e.g., a set of small primes). Recently Coron, Naccache and Stern [9] showed that a stronger form of this type of attack could be quite effective against some instances of the ISO/IEC 9796-2 signature scheme. They also analyzed the complexity of this type of attack against the EMSA-PKCS1-v1\_5 encoding method and concluded that an attack would be impractical, requiring more operations than a collision search on the underlying hash function (i.e., more than  $2^{80}$  operations). Coron *et al.*'s attack was subsequently extended by Coppersmith, Halevi and Jutla [8] to break the ISO/IEC 9769-1 signature scheme with message recovery. The various attacks illustrate the importance of carefully constructing the input to the RSA signature primitive, particularly in a signature scheme with message recovery. Accordingly, the EMSA-PKCS1-v1\_5 encoding method explicitly includes a hash operation and is not intended for signature schemes with message recovery. Moreover, while no attack is known against the EMSA-PKCS1-v1\_5 encoding method, a gradual transition to EMSA-PSS is recommended as a precaution against future developments.

2. The signature generation and verification operation operations are readily implemented as “single-pass” operations if the signature is placed after the message. See PKCS #7 [28] for an example format.

### 8.1.1 Signature generation operation

RSASSA-PKCS1-v1\_5-SIGN ( $K, M$ )

*Input:*         $K$         signer's RSA private key

$M$         message to be signed, an octet string

*Output:*         $S$         signature, an octet string of length  $k$ , where  $k$  is the length in octets of the modulus  $n$

*Errors:*        “message too long”; “modulus too short”

*Steps:*

1. Apply the EMSA-PKCS1-v1\_5 encoding operation (Section 9.2.1) to the message  $M$  to produce an encoded message  $EM$  of length  $k-1$  octets:

$$EM = \text{EMSA-PKCS1-v1\_5-ENCODE}(M, k-1) .$$

If the encoding operation outputs “message too long,” then output “message too long” and stop. If the encoding operation outputs “intended encoded message length too short,” then output “modulus too short” and stop.

- Convert the encoded message  $EM$  to an integer message representative  $m$ :

$$m = \text{OS2IP}(EM) .$$

- Apply the RSASP1 signature primitive (Section 5.2.1) to the private key  $K$  and the message representative  $m$  to produce an integer signature representative  $s$ :

$$s = \text{RSASP1}(K, m) .$$

- Convert the signature representative  $s$  to a signature  $S$  of length  $k$  octets:

$$S = \text{I2OSP}(s, k) .$$

- Output the signature  $S$ .

### 8.1.2 Signature verification operation

RSASSA-PKCS1-v1\_5-VERIFY  $((n, e), M, S)$

*Input:*  $(n, e)$  signer’s RSA public key

$M$  message whose signature is to be verified, an octet string

$S$  signature to be verified, an octet string of length  $k$ , where  $k$  is the length in octets of the modulus  $n$

*Output:* “valid signature” or “invalid signature”

*Errors:* “message too long”; “modulus too short”

*Steps:*

- Apply the EMSA-PKCS1-v1\_5 encoding operation (Section 9.2.1) to the message  $M$  to produce an encoded message  $EM$  of length  $k-1$  octets:

$$EM = \text{EMSA-PKCS1-v1\_5-ENCODE}(M, k-1) .$$

If the encoding operation outputs “message too long,” then output “message too long” and stop. If the encoding operation outputs “intended encoded message length too short,” then output “modulus too short” and stop.

2. If the length of the signature  $S$  is not  $k$  octets, output “invalid signature” and stop.
3. Convert the signature  $S$  to an integer signature representative  $s$ :

$$s = \text{OS2IP}(S) .$$

4. Apply the RSAVP1 verification primitive (Section 5.2.2) to the public key  $(n, e)$  and the signature representative  $s$  to produce an integer message representative  $m$ :

$$m = \text{RSAVP1}((n, e), s) .$$

If RSAVP1 outputs “signature representative out of range,” then output “invalid signature” and stop.

5. Convert the message representative  $m$  to a second encoded message  $EM$  of length  $k-1$  octets:

$$EM' = \text{I2OSP}(m, k-1) .$$

If I2OSP outputs “integer too large,” then output “invalid signature” and stop.

6. Compare the encoded message  $EM$  and the second encoded message  $EM'$ . If they are the same, output “valid signature”; otherwise, output “invalid signature.”

*Note.* Another way to implement the signature verification operation is to apply a decoding operation (not specified in this document) to the encoded message to recover the underlying hash value, and then to compare it to a newly computed hash value. This has the advantage that it requires less intermediate storage (two hash values rather than two encoded messages), but the disadvantage that it requires additional code.

## 8.2 RSASSA-PSS

RSASSA-PSS combines the RSASP1 and RSAVP1 primitives with the EMSA-PSS encoding method. It is compatible with the IFSSA scheme defined in the IEEE P1363 draft where the signature and verification primitives are IFSP-RSA1 and IFVP-RSA1 and the message encoding method is EMSA-PSS (which is not defined in the IEEE P1363 draft). The length of messages on which RSASSA-PSS can operate is either unrestricted or constrained by a very large number, depending on the hash function underlying the EMSA-PSS encoding method.

Assuming that the hash and mask generation functions in EMSA-PSS have appropriate properties and the key size is sufficiently large, RSASSA-PSS provides secure signatures. This assurance is provable in the sense that the difficulty of forging signatures can be directly related to the difficulty of inverting the RSA function, if the hash and mask generation functions are viewed as a black box or random oracle. In contrast to the RSASSA-PKCS1-v1\_5 signature scheme, a hash function identifier is not embedded in the encoded message, so in theory it is possible for an adversary to substitute a different hash

function than the one selected by the signer. However, this is not likely to be useful assuming that the mask generation function is based on the same hash function, since then the entire encoded message will be dependent on the selected hash function, not just the portion corresponding to the hash value as in EMSA-PKCS1-v1\_5.

RSASSA-PSS is different than other RSA-based signature schemes in that it is probabilistic rather than deterministic, incorporating a randomly generated salt value. The salt value enhances the security of the scheme by affording a more “tight” security proof than deterministic alternatives such as Full Domain Hashing (FDH) (see [3] for discussion). However, the randomness is not critical to security. In situations where random generation is not possible, a fixed value or a sequence number could be employed instead, with the resulting provable security similar to that of FDH. The randomness also reduces the requirements on the underlying hash function. Since an opponent does not know which salt value the signer will select, finding a collision in the hash function (two messages with the same hash value) does not enable an opponent to forge signatures. Accordingly, the collision-resistance of the hash function is not as important as in a deterministic signature scheme.

*Note.* The signature generation and verification operations are readily implemented as “single-pass” operations if the signature is placed after the message and the salt value produced by the signature generation operation is carried before it.

### 8.2.1 Signature generation operation

RSASSA-PSS-SIGN ( $K, M$ )

*Input:*             $K$         signer’s RSA private key

$M$         message to be signed, an octet string

*Output:*            $S$         signature, an octet string of length  $k$ , where  $k$  is the length in octets of the modulus  $n$

$salt$     (optional) salt value, an octet string of length  $hLen$

*Errors:*            “message too long”; “modulus too short”

*Steps:*

1.        Generate a random octet string  $salt$  of length  $hLen$ .
2.        Apply the EMSA-PSS encoding operation (Section 9.2.2) to the message  $M$  and the salt value to produce an encoded message  $EM$  of length  $k-1$  octets:

$$EM = \text{EMSA-PSS-ENCODE}(M, salt, k-1) .$$

If the encoding operation outputs “message too long,” then output “message too long” and stop. If the encoding operation outputs “intended encoded message length too short,” then output “modulus too short” and stop.

3. Convert the encoded message  $EM$  to an integer message representative  $m$ :

$$m = \text{OS2IP}(EM) .$$

4. Apply the RSASP1 signature primitive (Section 5.2.1) to the private key  $K$  and the message representative  $m$  to produce an integer signature representative  $s$ :

$$s = \text{RSASP1}(K, m) .$$

5. Convert the signature representative  $s$  to a signature  $S$  of length  $k$  octets:

$$S = \text{I2OSP}(s, k) .$$

6. Output the signature  $S$  and if desired the salt value.

### 8.2.2 Signature verification operation

RSASSA-PSS-VERIFY  $((n, e), M, S, [salt])$

*Input:*

- $(n, e)$  signer’s RSA public key
- $M$  message whose signature is to be verified, an octet string
- $S$  signature to be verified, an octet string of length  $k$ , where  $k$  is the length in octets of the modulus  $n$
- $salt$  (optional) salt value generated by RSASSA-PSS-SIGN, an octet string of length  $hLen$

*Output:* “valid signature” or “invalid signature”

*Errors:* “message too long”; “modulus too short”

*Steps:* (There are two cases, depending on whether the salt value is provided.)

*If the salt value is provided:*

1. Apply the EMSA-PSS encoding operation (Section 9.2.2) to the message  $M$  and the salt value to produce an encoded message  $EM$  of length  $k-1$  octets:

$$EM = \text{EMSA-PSS-ENCODE}(H, salt, k-1) .$$



If the encoding operation outputs “message too long,” then output “message too long” and stop. If the encoding operation outputs “intended encoded message length too short,” then output “modulus too short” and stop.

2. If the length of the signature  $S$  is not  $k$  octets, output “invalid signature” and stop.
3. Convert the signature  $S$  to an integer signature representative  $s$ :

$$s = \text{OS2IP}(S) .$$

4. Apply the RSAVP1 verification primitive (Section 5.2.2) to the public key  $(n, e)$  and the signature representative  $s$  to produce an integer message representative  $m$ :

$$m = \text{RSAVP1}((n, e), s) .$$

If RSAVP1 outputs “invalid,” then output “invalid signature” and stop.

5. Convert the message representative  $m$  to a second encoded message  $EM'$  of length  $k-1$  octets:

$$EM' = \text{I2OSP}(m, k-1) .$$

If I2OSP outputs “integer too large,” then output “invalid signature” and stop.

6. Compare the encoded message  $EM$  and the second encoded message  $EM'$ . If they are the same, output “valid signature”; otherwise, output “invalid signature.”

*If the salt value is not provided:*

1. If the length of the signature  $S$  is not  $k$  octets, output “invalid signature” and stop.
2. Convert the signature  $S$  to an integer signature representative  $s$ :

$$s = \text{OS2IP}(S) .$$

3. Apply the RSAVP1 verification primitive (Section 5.2.2) to the public key  $(n, e)$  and the signature representative  $s$  to produce an integer message representative  $m$ :

$$m = \text{RSAVP1}((n, e), s) .$$

If RSAVP1 outputs “invalid,” then output “invalid signature” and stop.

4. Convert the message representative  $m$  to an encoded message  $EM$  of length  $k-1$  octets:

$$EM = \text{I2OSP}(m, k-1) .$$

If I2OSP outputs “integer too large,” then output “invalid signature” and stop.

5. Apply the EMSA-PSS verification operation (Section 9.2.2.2) to the message  $M$  and the encoded message  $EM$  to determine whether they are consistent:

EMSA-PSS-VERIFY ( $M$ ,  $EM$ ) .

If the verification operation outputs “message too long,” then output “message too long” and stop. If the verification operation outputs “consistent,” then output “valid signature”; otherwise, output “invalid signature.”

*Note.* Another way to implement the signature verification operation in either case is to apply a decoding operation (not specified in this document) to the encoded message to recover the underlying hash and salt values, rather than applying the verification or encoding operation. The advantages and disadvantages are similar to those noted for EMSA-PKCS1-v1\_5.

## 9. Encoding methods

Encoding methods consist of operations that map between octet string messages and octet string encoded messages, which are converted to and from integer message representatives in the schemes. The integer message representatives are processed by the primitives. The encoding methods thus provide the connection between the schemes, which process messages, and the primitives.

Two types of encoding method are considered in this document: encoding methods for encryption and encoding methods for signatures with appendix.

### 9.1 Encoding methods for encryption

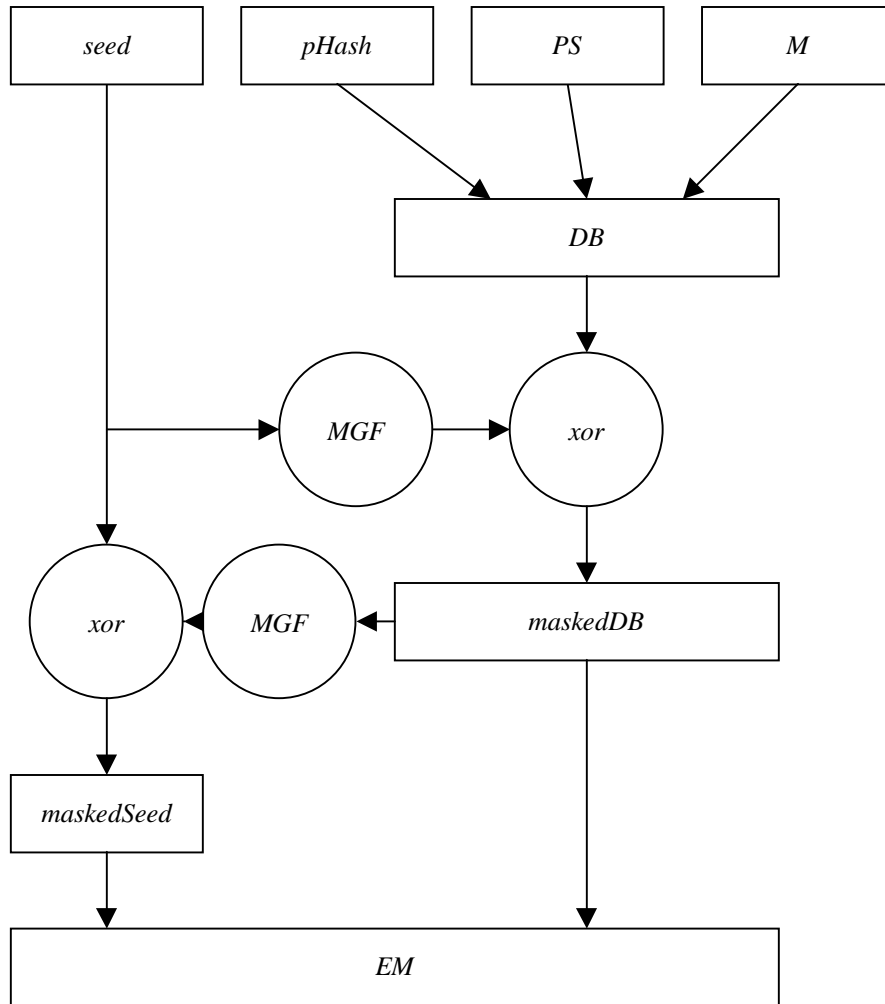
An encoding method for encryption consists of an *encoding operation* and a *decoding operation*. An encoding operation maps a message  $M$  to an encoded message  $EM$  of a specified length; the decoding operation maps an encoded message  $EM$  back to a message. The encoding and decoding operations are inverses.

The encoded message  $EM$  will typically have some structure that can be verified by the decoding operation. The decoding operation will output “decoding error” if the structure is not present. The encoding operation may also introduce some randomness, so that different applications of the encoding operation to the same message will produce encoded messages.

Two encoding methods for encryption are employed in the encryption schemes and are specified here: EME-OAEP and EME-PKCS1-v1\_5.

#### 9.1.1 EME-OAEP

This encoding method is parameterized by the choice of hash function and mask generation function. Suggested hash and mask generation functions are given in Appendix



**Figure 1: EME-OAEP encoding operation.** *pHash* is the hash of the optional encoding parameters. Decoding operation follows reverse steps to recover *M* and verify *pHash* and *PS*.

B. The encoding method is based on Bellare and Rogaway’s Optimal Asymmetric Encryption scheme [2]. (OAEP stands for “Optimal Asymmetric Encryption Padding.”) It is the same as the method in the IEEE P1363 draft except that it outputs an octet string rather than the corresponding integer, and that the length of the encoded message is expressed in octets rather than bits. Figure 1 illustrates the encoding operation.

**9.1.1.1 Encoding operation**

EME-OAEP-ENCODE (*M*, *P*, *emLen*)

*Options:*     *Hash* hash function (*hLen* denotes the length in octets of the hash function output)

*MGF* mask generation function

*Input:* *M* message to be encoded, an octet string of length at most  $emLen-1-2hLen$  ( $mLen$  denotes the length in octets of *M*)

*P* encoding parameters, an octet string

$emLen$  intended length in octets of the encoded message, at least  $2hLen+1$

*Output:* *EM* encoded message, an octet string of length  $emLen$

*Errors:* “message too long”; “parameter string too long”

*Steps:*

1. If the length of *P* is greater than the input limitation for the hash function ( $2^{61}-1$  octets for SHA-1) then output “parameter string too long” and stop.
2. If  $mLen > emLen-2hLen-1$ , output “message too long” and stop.
3. Generate an octet string *PS* consisting of  $emLen-mLen-2hLen-1$  zero octets. The length of *PS* may be 0.
4. Let  $pHash = Hash(P)$ , an octet string of length  $hLen$ .
5. Concatenate *pHash*, *PS*, the message *M*, and other padding to form a data block *DB* as
 
$$DB = pHash \parallel PS \parallel 01 \parallel M .$$
6. Generate a random octet string *seed* of length  $hLen$ .
7. Let  $dbMask = MGF(seed, emLen-hLen)$ .
8. Let  $maskedDB = DB \text{ xor } dbMask$ .
9. Let  $seedMask = MGF(maskedDB, hLen)$ .
10. Let  $maskedSeed = seed \text{ xor } seedMask$ .
11. Let  $EM = maskedSeed \parallel maskedDB$ .
12. Output *EM*.

### 9.1.1.2 Decoding operation

EME-OAEP-DECODE (*EM*, *P*)

*Options:*     *Hash* hash function (*hLen* denotes the length in octets of the hash function output)

*MGF* mask generation function

*Input:*        *EM* encoded message, an octet string of length at least  $2hLen+1$  (*emLen* denotes the length in octets of *EM*)

*P* encoding parameters, an octet string

*Output:*       *M* recovered message, an octet string of length at most  $emLen-1-2hLen$

*Errors:*       “decoding error”

*Steps:*

1. If the length of *P* is greater than the input limitation of the hash function ( $2^{61}-1$  octets for SHA-1) then output “decoding error” and stop.
2. If  $emLen < 2hLen+1$ , output “decoding error” and stop.
3. Let *maskedSeed* be the first *hLen* octets of *EM* and let *maskedDB* be the remaining  $emLen-hLen$  octets.
4. Let  $seedMask = MGF(maskedDB, hLen)$ .
5. Let  $seed = maskedSeed \text{ xor } seedMask$ .
6. Let  $dbMask = MGF(seed, emLen-hLen)$ .
7. Let  $DB = maskedDB \text{ xor } dbMask$ .
8. Let  $pHash = Hash(P)$ , an octet string of length *hLen*.
9. Separate *DB* into an octet string *pHash'* consisting of the first *hLen* octets of *DB*, a (possibly empty) octet string *PS* consisting of consecutive zero octets following *pHash'*, and a message *M* as

$$DB = pHash' \parallel PS \parallel 01 \parallel M .$$

If there is no 01 octet to separate *PS* from *M*, output “decoding error” and stop.

10. If *pHash'* does not equal *pHash*, output “decoding error” and stop.
11. Output *M*.



2. Separate the encoded message  $EM$  into an octet string  $PS$  consisting of nonzero octets and a message  $M$  as

$$EM = 02 \parallel PS \parallel 00 \parallel M .$$

If the first octet of  $EM$  is not 02, or if there is no 00 octet to separate  $PS$  from  $M$ , output “decoding error” and stop.

3. If the length of  $PS$  is less than 8 octets, output “decoding error” and stop.
4. Output  $M$ .

## 9.2 Encoding methods for signatures with appendix

An *encoding method for signatures with appendix*, for the purposes of this document, consists of an encoding operation and optionally a verification operation. An encoding operation maps a message  $M$  to an encoded message  $EM$  of a specified length. A verification operation determines whether a message  $M$  and an encoded message  $EM$  are consistent, i.e., whether the encoded message  $EM$  is a valid encoding of the message  $M$ .

The encoding operation may introduce some randomness, so that different applications of the encoding operation to the same message will produce different encoded messages, which has benefits for provable security. For such an encoding method, both an encoding and a verification operation are needed unless the randomness can be reproduced by the verifier (e.g., by obtaining the salt value from the signer). For a deterministic encoding method only an encoding operation is needed.

Two encoding methods for signatures with appendix are employed in the signature schemes and are specified here: EMSA-PKCS1-v1\_5 and EMSA-PSS.

### 9.2.1 EMSA-PKCS1-v1\_5

This encoding method is deterministic and only has an encoding operation.

EMSA-PKCS1-v1\_5-ENCODE ( $M$ ,  $emLen$ )

*Option:*        *Hash*    hash function ( $hLen$  denotes the length in octets of the hash function output)

*Input:*         $M$         message to be encoded

$emLen$  intended length in octets of the encoded message, at least  $\lceil T \rceil + 10$ , where  $T$  is the DER encoding of a certain value computed during the encoding operation

*Output:*         $EM$         encoded message, an octet string of length  $emLen$

*Errors:* “message too long”; “intended encoded message length too short”

*Steps:*

1. Apply the hash function to the message  $M$  to produce a hash value  $H$ :

$$H = \text{Hash}(M).$$

If the hash function outputs “message too long,” then output “message too long” and stop.

2. Encode the algorithm ID for the hash function and the hash value into an ASN.1 value of type `DigestInfo` (see Section A) with the Distinguished Encoding Rules (DER), where the type `DigestInfo` has the syntax

```
DigestInfo ::= SEQUENCE {
    digestAlgorithm AlgorithmIdentifier,
    digest OCTET STRING }
```

The first field identifies the hash function and the second contains the hash value. Let  $T$  be the DER encoding.<sup>1</sup>

3. If  $emLen < \|T\| + 10$ , output “intended encoded message length too short” and stop.
4. Generate an octet string  $PS$  consisting of  $emLen - \|T\| - 2$  octets with value FF (hexadecimal). The length of  $PS$  will be at least 8 octets.
5. Concatenate  $PS$ , the DER encoding  $T$ , and other padding to form the encoded message  $EM$  as

$$EM = 01 \| PS \| 00 \| T .$$

6. Output  $EM$ .

### 9.2.2 EMSA-PSS

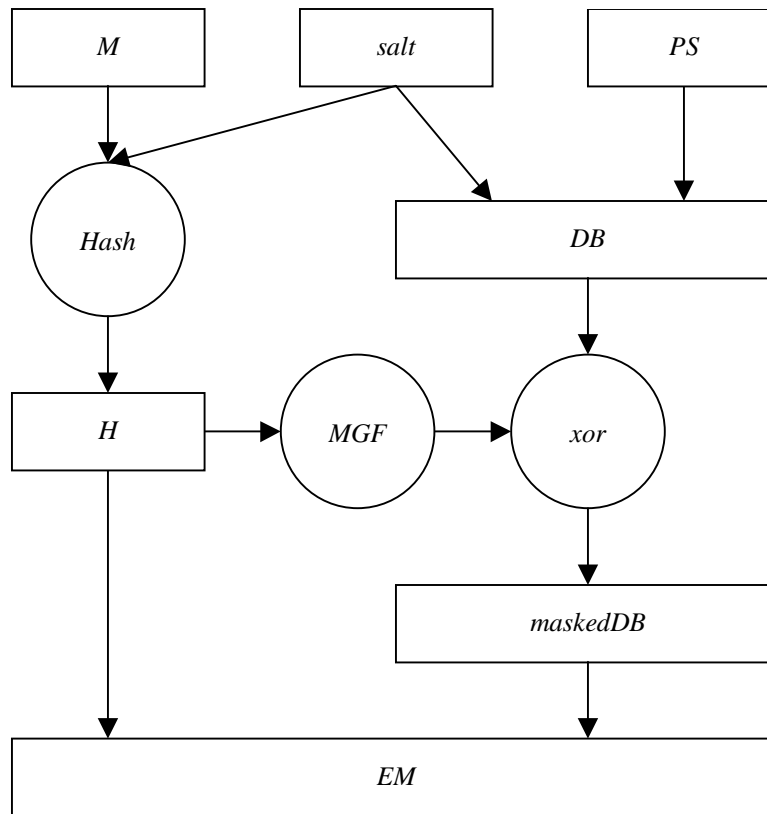
This encoding method is parameterized by the choice of hash function and mask generation function. Suggested hash and mask generation functions are given in Appendix B. The encoding method is based on Bellare and Rogaway’s Probabilistic Signature

---

<sup>1</sup> For the three hash functions mentioned in Appendix B.1, this step is equivalent to the following:

For MD2:  $T = 30\ 20\ 30\ 0c\ 06\ 08\ 2a\ 86\ 48\ 86\ f7\ 0d\ 02\ 02\ 05\ 00\ 04\ 10 \| H .$   
 For MD5:  $T = 30\ 20\ 30\ 0c\ 06\ 08\ 2a\ 86\ 48\ 86\ f7\ 0d\ 02\ 05\ 05\ 00\ 04\ 10 \| H .$   
 For SHA-1:  $T = 30\ 21\ 30\ 1f\ 06\ 05\ 2b\ 0e\ 03\ 02\ 1a\ 05\ 00\ 04\ 14 \| H .$





**Figure 2: EMSA-PSS encoding operation.** Verification operation follows reverse steps to recover *salt*, then forward steps to recompute and compare *H*.

Scheme (PSS) [3][4]. It is randomized and has an encoding operation and a verification operation. [Figure 2](#) illustrates the encoding operation.

*Notes.*

1. The encoding method defined here differs from the one in Bellare and Rogaway's submission [4] in two respects. First, it applies a hash function to the message rather than a mask generation function. Even though the mask generation function is based on a hash function, it seems more natural to apply the hash function directly. Second, the salt value is an input to the operation, rather than an internal value. This facilitates "one-pass" processing (see notes to Section 8.2), particularly in the case of signature verification. (Also, the name "salt" is used instead of "seed", as it is more reflective of the value's role.)
2. The salt value is a fixed length for a given hash function in this encoding method, thereby avoiding the need for including the salt length in the input to the hash function as discussed in [4].
3. Assuming that the mask generation is based on a hash function, it is recommended that the hash function be the same as the one that is applied to the message. In this way, the entire encoded message will be dependent on the same hash function and it will be difficult for an opponent to substitute a different hash function than the one intended by the signer (see Section 8.2). However, this matching of hash functions is not strictly necessary for security.

**9.2.2.1 Encoding operation**EMSA-PSS-ENCODE ( $M$ ,  $salt$ ,  $emLen$ )

*Options:*     *Hash* hash function ( $hLen$  denotes the length in octets of the hash function output)

*MGF* mask generation function

*Input:*        *M*       message to be encoded, an octet string

*salt*     salt value, an octet string of length  $hLen$

*emLen* intended length in octets of the encoded message, at least  $2hLen$

*Output:*        *EM*     encoded message, an octet string of length  $emLen$

*Errors:*        “message too long”; “intended encoded message length too short”

*Steps:*

1.     If  $emLen < 2hLen$ , output “intended encoded message length too short” and stop.
2.     Apply the hash function to the salt value and the message  $M$  to produce a hash value  $H$ :

$$H = Hash (salt || M) .$$

If the hash function outputs “message too long,” then output “message too long” and stop.

3.     Generate an octet string  $PS$  consisting of  $emLen - 2hLen$  zero octets. The length of  $PS$  may be 0.
4.     Concatenate  $salt$  and  $PS$  to form a data block  $DB$  as

$$DB = salt || PS .$$

5.     Let  $dbMask = MGF (H, emLen - hLen)$ .
6.     Let  $maskedDB = DB \text{ xor } dbMask$ .
7.     Let  $EM = H || maskedDB$ .
8.     Output  $EM$ .

**9.2.2.2 Verification operation**EMSA-PSS-VERIFY ( $M$ ,  $EM$ )

*Options:*     *Hash* hash function ( $hLen$  denotes the length in octets of the hash function output)

*MGF* mask generation function

*Input:*        *M*       message to be verified

*EM*       encoded message to be verified, an octet string of length at least  $2hLen$  ( $emLen$  denotes the length in octets of  $EM$ )

*Output:*       “consistent” or “inconsistent”

*Errors:*       “message too long”; “encoded message too short”

*Steps:*

1.     If  $emLen < 2hLen$ , output “encoded message too short” and stop.
2.     Let  $H$  be the first  $hLen$  octets of  $EM$  and let  $maskedDB$  be the remaining  $emLen - hLen$  octets.
3.     Let  $dbMask = MGF(H, emLen - hLen)$ .
4.     Let  $DB = maskedDB \text{ xor } dbMask$ .
5.     Let  $salt$  be the first  $hLen$  octets of  $DB$  and let  $PS$  be the remaining  $emLen - 2hLen$  octets.
7.     If  $PS$  does not consist of  $emLen - 2hLen$  zero octets, output “inconsistent” and stop.
8.     Apply the hash function to the salt and the message  $M$  to produce a second hash value  $H'$ :

$$H' = Hash(salt || M) .$$

If the hash function outputs “message too long,” then output “message too long” and stop.

9.     If  $H'$  equals  $H$ , then output “consistent”; otherwise output “inconsistent.”

## A. ASN.1 syntax

[[This section may be updated to improve the presentation of the ASN.1 syntax.]]

### A.1 Key representation

This section defines ASN.1 object identifiers for RSA public and private keys, and defines the types `RSAPublicKey` and `RSAPrivateKey`. The intended application of these definitions includes X.509 certificates, PKCS #8 [29], and PKCS #12 [30].

The object identifier `rsaEncryption` identifies RSA public and private keys as defined in Appendices A.1.1 and A.1.2. The `parameters` field associated with this OID in an `AlgorithmIdentifier` shall have type `NULL`.

```
rsaEncryption OBJECT IDENTIFIER ::= {pkcs-1 1}
```

All of the definitions in this section are the same as in PKCS #1 v1.5.

#### A.1.1 Public-key syntax

An RSA public key should be represented with the ASN.1 type `RSAPublicKey`:

```
RSAPublicKey ::= SEQUENCE {
    modulus INTEGER, -- n
    publicExponent INTEGER -- e }
```

(This type is specified in X.509 and is retained here for compatibility.)

The fields of type `RSAPublicKey` have the following meanings:

- `modulus` is the modulus  $n$ .
- `publicExponent` is the public exponent  $e$ .

#### A.1.2 Private-key syntax

An RSA private key should be represented with ASN.1 type `RSAPrivateKey`:

```
RSAPrivateKey ::= SEQUENCE {
    version Version,
    modulus INTEGER, -- n
    publicExponent INTEGER, -- e
    privateExponent INTEGER, -- d
    prime1 INTEGER, -- p
    prime2 INTEGER, -- q
    exponent1 INTEGER, -- d mod (p-1)
```

```

exponent2 INTEGER, -- d mod (q-1)
coefficient INTEGER -- (inverse of q) mod p }

```

```
Version ::= INTEGER
```

The fields of type `RSAPrivateKey` have the following meanings:

- `version` is the version number, for compatibility with future revisions of this document. It shall be 0 for this version of the document.
- `modulus` is the modulus  $n$ .
- `publicExponent` is the public exponent  $e$ .
- `privateExponent` is the private exponent  $d$ .
- `prime1` is the prime factor  $p$  of  $n$ .
- `prime2` is the prime factor  $q$  of  $n$ .
- `exponent1` is  $d \bmod (p-1)$ .
- `exponent2` is  $d \bmod (q-1)$ .
- `coefficient` is the Chinese Remainder Theorem coefficient  $q^{-1} \bmod p$ .

## A.2 Scheme identification

This section defines object identifiers for the encryption and signature schemes. The schemes compatible with PKCS #1 v1.5 have the same definitions as in PKCS #1 v1.5. The intended application of these definitions includes X.509 certificates and PKCS #7.

### A.2.1 RSAES-OAEP

The object identifier `id-RSAES-OAEP` identifies the RSAES-OAEP encryption scheme.

```
id-RSAES-OAEP OBJECT IDENTIFIER ::= {pkcs-1 7}
```

The `parameters` field associated with this OID in an `AlgorithmIdentifier` shall have type `RSAES-OAEP-params`:

```

RSAES-OAEP-params ::= SEQUENCE {
  hashFunc [0] AlgorithmIdentifier {{oaepDigestAlgorithms}}
    DEFAULT sha1Identifier,
  maskGenFunc [1] AlgorithmIdentifier {{pkcs1MGFAlgorithms}}
    DEFAULT mgf1SHA1Identifier,
  pSourceFunc [2] AlgorithmIdentifier

```

```
{pkcs1pSourceAlgorithms}
DEFAULT pSpecifiedEmptyIdentifier }
```

The fields of type RSAES-OAEP-params have the following meanings:

- `hashFunc` identifies the hash function. It shall be an algorithm ID with an OID in the set `oaepDigestAlgorithms`, which for this version shall consist of `id-sha1`, identifying the SHA-1 hash function (see Appendix B.1).

```
oaepDigestAlgorithms ALGORITHM-IDENTIFIER ::= {
  {NULL IDENTIFIED BY id-sha1} }
```

The default hash function is SHA-1:

```
sha1Identifier ::= AlgorithmIdentifier {id-sha1, NULL}
```

- `maskGenFunc` identifies the mask generation function. It shall be an algorithm ID with an OID in the set `pkcs1MGFAlgorithms`, which for this version shall consist of `id-mgf1`, identifying the MGF1 mask generation function (see Appendix B.2.1). The `parameters` field for `id-mgf1` shall be an algorithm ID with an OID in the set `oaepDigestAlgorithms`, identifying the hash function on which MGF1 is based.

```
pkcs1MGFAlgorithms ALGORITHM-IDENTIFIER ::= {
  {AlgorithmIdentifier {{oaepDigestAlgorithms}} IDENTIFIED
  BY id-mgf1} }
```

The default mask generation function is MGF1 with SHA-1:

```
mgf1SHA1Identifier ::= AlgorithmIdentifier {
  id-mgf1, sha1Identifier }
```

- `pSourceFunc` identifies the source (and possibly the value) of the encoding parameters  $P$ . It shall be an algorithm ID with an OID in the set `pkcs1pSourceAlgorithms`, which for this version shall consist of `id-pSpecified`, indicating that the encoding parameters are specified explicitly. The `parameters` field for `id-pSpecified` shall have type OCTET STRING, containing the encoding parameters.

```
pkcs1pSourceAlgorithms ALGORITHM-IDENTIFIER ::= {
  {OCTET STRING IDENTIFIED BY id-pSpecified} }
```

```
id-pSpecified OBJECT IDENTIFIER ::= {pkcs-1 9}
```

The default encoding parameters is an empty string (so that  $pHash$  in EME-OAEP will contain the hash of the empty string):

```
pSpecifiedEmptyIdentifier ::= AlgorithmIdentifier {
  id-pSpecified, OCTET STRING SIZE (0) }
```

If all of the default values of the fields in `RSAES-OAEP-params` are used, then the algorithm identifier will have the following value:

```
RSAES-OAEP-Default-Identifier ::= AlgorithmIdentifier {
  id-RSAES-OAEP,
  {sha1Identifier,
   mgf1SHA1Identifier,
   pSpecifiedEmptyIdentifier } }
```

### A.2.2 RSAES-PKCS1-v1\_5

The object identifier `rsaEncryption` (Appendix A.1) identifies the RSAES-PKCS1-v1\_5 encryption scheme. The `parameters` field associated with this OID in an `AlgorithmIdentifier` shall have type `NULL`. This is the same as in PKCS #1 v1.5.

```
rsaEncryption OBJECT IDENTIFIER ::= {pkcs-1 1}
```

### A.2.3 RSASSA-PKCS1-v1\_5

The object identifier for RSASSA-PKCS1-v1\_5 shall be one of the following. The choice of OID depends on the choice of hash algorithm: MD2, MD5 or SHA-1. Note that if either MD2 or MD5 is used then the OID is just as in PKCS #1 v1.5. For each OID, the `parameters` field associated with this OID in an `AlgorithmIdentifier` shall have type `NULL`.

If the hash function to be used is MD2, then the OID should be:

```
md2WithRSAEncryption ::= {pkcs-1 2}
```

If the hash function to be used is MD5, then the OID should be:

```
md5WithRSAEncryption ::= {pkcs-1 4}
```

If the hash function to be used is SHA-1, then the OID should be:

```
sha1WithRSAEncryption ::= {pkcs-1 5}
```

### A.2.4 RSASSA-PSS

The object identifier `id-RSASSA-PSS` identifies the RSASSA-PSS encryption scheme.

```
id-RSASSA-PSS OBJECT IDENTIFIER ::= {pkcs-1 10}
```

The `parameters` field associated with this OID in an `AlgorithmIdentifier` shall have type `RSASSA-PSS-params`:

```
RSASSA-PSS-params ::= SEQUENCE {
    hashFunc [0] AlgorithmIdentifier {{oaepDigestAlgorithms}}
        DEFAULT sha1Identifier,
    maskGenFunc [1] AlgorithmIdentifier {{pkcs1MGFAlgorithms}}
        DEFAULT mgf1SHA1Identifier,
    salt OCTET STRING OPTIONAL }
```

The fields of type RSASSA-PSS-params have the following meanings:

- `hashFunc` identifies the hash function. It shall be an algorithm ID with an OID in the set `oaepDigestAlgorithms` (see Appendix A.2.1). The default hash function is SHA-1.
- `maskGenFunc` identifies the mask generation function. It shall be an algorithm ID with an OID in the set `pkcs1MGFAlgorithms` (see Appendix A.2.1). The default mask generation function is MGF1 with SHA-1.
- `salt` is the salt value associated with the signature operation. The field is intended to facilitate single-pass processing (see Section 8.2). If the field is omitted, the salt value shall be obtained from the signature.

If the default value of the `hashFunc` and `maskGenFunc` fields of RSASSA-PSS-params are used and the `seed` field is omitted, then the algorithm identifier will have the following value:

```
RSASSA-PSS-Default-Identifier ::= AlgorithmIdentifier {
    id-RSASSA-PSS,
    { sha1Identifier, mgf1SHA1Identifier } }
```

*Note.* In some applications, the hash function underlying a signature scheme is identified separately from the signature scheme itself. For instance, in PKCS #7 [28] and S/MIME CMS [18], a hash algorithm identifier is placed before the message and a signature algorithm identifier is placed after it. To enable single-pass processing for RSASSA-PSS in such applications, the hash algorithm identifier should contain the salt value (in which case the signature algorithm identifier does not need to contain it). Accordingly, the object identifier `id-salted-hash` is provided to specify a salt value as well as a hash function:

```
id-salted-hash ::= {pkcs-1 11}
```

The parameters field associated with this OID in an `AlgorithmIdentifier` shall have type `Salted-Hash_Params`:

```
Salted-Hash_Params ::= SEQUENCE {
    hashFunc [0] AlgorithmIdentifier,
    salt OCTET STRING OPTIONAL }
```

The field `hashFunc` identifies the underlying hash function and the field `salt` is the salt value.



PSS can thus be supported in PKCS #7 and S/MIME CMS, by specifying `id-salted-hash` with the salt value as the hash algorithm identifier and `id-RSASSA-PSS` without the salt value as the signature algorithm identifier.

In one mode of both PKCS #7 and S/MIME CMS, the hash function is applied twice, once to the message and again to an attribute set that contains the hash of the message. The same hash function is applied in each case. Consequently, if a salted hash function is specified then it should be applied with the same salt both times. (This does not impact the security of the RSASSA-PSS scheme.)

(In new applications, it would be preferable to place the full signature algorithm identifier before the message rather than a hash algorithm identifier, because it may not always be possible to separate a signature algorithm from an underlying hash function.)

## B. Supporting techniques

This section gives several examples of underlying functions supporting the encoding methods in Sections 09. While these supporting techniques are appropriate for applications to implement, none of them is required to be implemented. It is expected, however, that profiles for PKCS #1 v2.0 will be developed that specify particular supporting techniques.

This section also gives object identifiers for the supporting techniques.

### B.1 Hash functions

Hash functions are used in the operations contained in Sections 7 and 8. Hash functions are deterministic, meaning that the output is completely determined by the input. Hash functions take octet strings of variable length, and generate fixed length octet strings. The hash functions used in the operations contained in Sections 7 and 8 should generally be *collision resistant*. This means that it is infeasible to find two distinct inputs to the hash function that produce the same output. A collision resistant hash function also has the desirable property of being *one-way*; this means that given an output, it is infeasible to find an input whose hash is the specified output. The property of collision resistance is especially desirable for RSASSA-PKCS1-v1\_5, as it makes it infeasible to forge signatures. For RSASSA-PSS, however, the property is less important, particularly if a random salt value is employed. In addition to the requirements, the hash function should yield a mask generation function (Appendix B.2) with pseudorandom output.

Three hash functions are recommended for the encoding methods in this document: MD2 [20], MD5 [24], and SHA-1 [22]. For the EME-OAEP and EMSA-PSS encoding methods, only SHA-1 is recommended. For the EMSA-PKCS1-v1\_5 encoding method, SHA-1 is recommended for new applications. MD2 and MD5 are recommended only for compatibility with existing applications based on PKCS #1 v1.5.

The hash functions themselves are not defined here; readers are referred to the appropriate references ([20], [24] and [22]).

The object identifiers `id-sha1`, `md2` and `md5` identify the respective hash functions:

```
id-SHA1 OBJECT IDENTIFIER ::=
    {iso(1) identified-organization(3) oiw(14) secsig(3)
     algorithms(2) 26 }
```

```
md2 OBJECT IDENTIFIER ::=
    {iso(1) member-body(2) us(840) rsadsi(113549)
     digestAlgorithm(2) 2 }
```

```
md5 OBJECT IDENTIFIER ::=
    {iso(1) member-body(2) us(840) rsadsi(113549)
     digestAlgorithm(2) 5 }
```

The `parameters` field associated with these OIDs in an `AlgorithmIdentifier` shall have type `NULL`.

*Note.* Version 1.5 of this document also allowed for the use of MD4 in signature schemes. The cryptanalysis of MD4 has progressed significantly in the intervening years. For example, Dobbertin [12] demonstrated how to find collisions for MD4 and that the first two rounds of MD4 are not one-way [14]. Because of these results and others (e.g. [11]), MD4 is no longer recommended. There have also been advances in the cryptanalysis of MD2 and MD5, although not enough to warrant removal from existing applications. Rogier and Chauvaud [26] demonstrated how to find collisions in a modified version of MD2. No one has demonstrated how to find collisions for the full MD5 algorithm, although partial results have been found (e.g. [8]). For new applications, to address these concerns, SHA-1 is preferred.

## B.2 Mask generation functions

A mask generation function takes an octet string of variable length and a desired output length as input, and outputs an octet string of the desired length. There may be restrictions on the length of the input and output octet strings, but such bounds are generally very large. Mask generation functions are deterministic; the octet string output is completely determined by the input octet string. The output of a mask generation function should be pseudorandom, that is, if the seed to the function is unknown, it should be infeasible to distinguish the output from a truly random string. The provable security of RSAES-OAEP and RSASSA-PSS relies on the random nature of the output of the mask generation function, which in turn relies on the random nature of the underlying hash.

One mask generation function is recommended for the encoding methods in this document, and is defined here: MGF1, which is based on a hash function. Future versions of this document may define other mask generation functions.

### B.2.1 MGF1

MGF1 is a Mask Generation Function based on a hash function.

MGF1 ( $Z, l$ )

*Options:*     *Hash* hash function (*hLen* denotes the length in octets of the hash function output)

*Input:*       *Z*       seed from which mask is generated, an octet string  
                   *l*       intended length in octets of the mask, at most  $2^{32} hLen$

*Output:*       *mask* mask, an octet string of length *l*

*Error:*        “mask too long”

*Steps:*

1.     If  $l > 2^{32} hLen$ , output “mask too long” and stop.
2.     Let *T* be the empty octet string.
3.     For *counter* from 0 to  $\lceil l/hLen \rceil - 1$ , do the following:
  - a.     Convert *counter* to an octet string *C* of length 4 with the primitive I2OSP:
 
$$C = \text{I2OSP}(\text{counter}, 4).$$
  - b.     Concatenate the hash of the seed *Z* and *C* to the octet string *T*:
 
$$T = T \parallel \text{Hash}(Z \parallel C).$$
4.     Output the leading *l* octets of *T* as the octet string *mask*.

The object identifier `id-mgf1` identifies the MGF1 mask generation function:

`id-mgf1 OBJECT IDENTIFIER ::= {pkcs-1 8}`

The `parameters` field associated with this OID in an `AlgorithmIdentifier` shall have type `AlgorithmIdentifier`, identifying the hash function on which MGF1 is based.

## C. ASN.1 module

[[to be added]]

## D. Intellectual property considerations

The RSA public-key cryptosystem is protected by U.S. Patent 4,405,829. RSA Security Inc. makes no other patent claims on the constructions described in this document, although specific underlying techniques may be covered.

The University of California has indicated that it has a patent pending on the PSS signature scheme [4]. It has also provided a letter to the IEEE P1363 working group stating that if the PSS signature scheme is included in an IEEE standard, “the University of California will, when that standard is adopted, FREELY license any conforming implementation of PSS as a technique for achieving a digital signature with appendix.” [16].

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## **E. Revision history**

### **Versions 1.0–1.3**

Versions 1.0–1.3 were distributed to participants in RSA Data Security, Inc.’s Public-Key Cryptography Standards meetings in February and March 1991.

### **Version 1.4**

Version 1.4 was part of the June 3, 1991 initial public release of PKCS. Version 1.4 was published as NIST/OSI Implementors’ Workshop document SEC-SIG-91-18.

### **Version 1.5**

Version 1.5 incorporated several editorial changes, including updates to the references and the addition of a revision history. The following substantive changes were made:

- Section 10: “MD4 with RSA” signature and verification processes were added.
- Section 11: `md4WithRSAEncryption` object identifier was added.

### **Version 2.0**

Version 2.0 incorporated major editorial changes in terms of the document structure and introduced the RSAEP-OAEP encryption scheme. This version continued to support the encryption and signature processes in version 1.5, although the hash algorithm MD4 is no longer allowed due to cryptanalytic advances in the intervening years. Version 2.0 was also published as IETF RFC 2437 [22].

### **Version 2.1**

Version 2.1 introduces the RSASSA-PSS signature scheme with appendix and incorporates several editorial improvements. This version continues to support the schemes in version 2.0.

## F. References

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## G. About PKCS

The *Public-Key Cryptography Standards* are specifications produced by RSA Laboratories in cooperation with secure systems developers worldwide for the purpose of accelerating the deployment of public-key cryptography. First published in 1991 as a result of meetings with a small group of early adopters of public-key technology, the PKCS documents have become widely referenced and implemented. Contributions from the PKCS series have become part of many formal and *de facto* standards, including ANSI X9 documents, PKIX, SET, S/MIME, and SSL.

Further development of PKCS occurs through mailing list discussions and occasional workshops, and suggestions for improvement are welcome. For more information, contact:

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